| Year 6 maths - Week Beginning 04.05.20 |  |  |  |  |  |
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| Theme | Geometry lesson 1 <br> Investigating opposite angles | Geometry lesson 2 Investigating angles in triangles | Geometry lesson 3 Investigating angles in quadrilaterals | Geometry lesson 4 Solving problems involving angles in triangles and quadrilaterals | Geometry lesson 5 Investigating circles |
| Factual fluency (to aid fluency) | Measure angles using a protractor here | Find missing angles here | Find missing angles (2) here | Find missing angles (3) here | Find missing angles (4) here |
| Problem/ activity of the day | (Lesson 1 resources below) MAKING LINKS: In year 5, we investigated angles on a line see here and at a point see here <br> THINK: (support below) <br> My friend says that when 2 straight lines cross, it creates opposite angles that are equal. <br> Do you agree/disagree? <br> Can you prove it? <br> SEE: (model below) <br> Watch lesson video here. <br> DO: Use what you have learned today to solve the problems. | (Lesson 2 resources below) MAKING LINKS: In year 4 and 5, we learnt the properties of different types of triangles. Use this link as a reminder. <br> THINK: (support below) <br> My friend says the angles in a triangle always add up to $180^{\circ}$. <br> Do you agree/disagree? <br> Can you prove it? <br> SEE: (model below) <br> Watch lesson video here. <br> DO: Use your knowledge of isosceles triangles and what you have learned today to solve the problems. | (Lesson 3 resources below) MAKING LINKS: In year 4 and 5, we learnt the properties of quadrilaterals. Use this link as a reminder. <br> THINK: (support below) <br> My friend says the angles in a quadrilateral always add up to $360^{\circ}$. <br> Do you agree/disagree? Can you prove it? <br> Tip: Yesterday we learnt that the sum of the angles in a triangle is $180^{\circ}$. Does this help? <br> SEE: (model below) <br> Watch lesson video here. <br> DO: Use your knowledge of isosceles triangles and what you have learned today to solve the problems. <br> Remember: parallelograms have 2 pairs of opposite angles that are equal. See here for more. | (Lesson 4 resources below) MAKING LINKS: On Tuesday and Wednesday, we solved problems involving angles in triangles and quadrilaterals. <br> THINK: (support below) <br> My friend thinks she can work out the size of angles in regular pentagons and hexagons without a protractor <br> Do you agree/disagree? Can you do it? <br> Tip: Pentagons and hexagons are made up of triangles and quadrilaterals. <br> SEE: (model below) <br> Watch lesson video here. <br> DO: Use what you have learned today to solve the problems. <br> Remember: the sum of the angles in a triangle is $180^{\circ}$. <br> Remember: the sum of the angles in a quadrilateral is $360^{\circ}$. | (Lesson 5 resources below) MAKING LINKS: In year 4 and 5 , we learnt the properties of shapes. <br> THINK: (support below) <br> A circle has a diameter, a radius and a circumference. See below or click here for more. <br> What is the relationship between the diameter and the radius? <br> What kind of triangle is created in the circle above? How do you know? <br> SEE: (model below) <br> Watch lesson video here. <br> DO: Use what you have learned today to solve the problems. |
| Time to check | Day 1 resources and answers (below) | Day 2 resources and answers (below) | Day 3 resources and answers (below) | Day 4 resources and answers (below) | Day 5 resources and answers (below) |

THINK: My friend says that when 2 straight lines cross, it creates opposite angles that are equal.


Get two pencils (or anything straight) and make them cross at a point. Move the pencils to see how the angles change. What do you notice? After drawing lots of straight lines that cross you could cut along one of the lines and rotate it $180^{\circ}$ so that it points in the opposite direction and lay it on top of its opposite angle. Can you work out why they are equal? You can rotate intersecting lines to see why here
SEE: lesson video here.


When I rotate my figure, I see that both sides of the straight lines HAVE EQUAL ANGLES

When I use a protractor to measure the opposite angles, I find THEY ARE EQUAL

The diagram to the left (bottom) shows $a+b=180$ and angle $b+c=180$ so angle $a=$ angle $c$

KEY POINT: Straight lines that cross create two pairs of equal opposite angles

## MAKING CONNECTIONS:

I can see that all 4 angles add up to $360^{\circ}$.
$100+100+80+80=360$
I can see that angles on a straight line add up to $180^{\circ}$. $80+100=180$ and $100+80=180$

## DO: Solve these problems

1. Which angles are equivalent?
 angle $\square$ = angle $\square$ and angle $\square$ =angle $\square$
2. Find the missing angles
angle $b=$
angle $c=$
angle $d=$

3. Find the missing angles


TOP TIPS: Look for $90^{\circ}$ symbol $490^{\circ}$. Opposite angles are equal. Angles on a straight line add up to $180^{\circ}$.

A whole turn is $360^{\circ}$.
It might help you if you write the information that you know in the diagram.

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THINK: My friend says the angles in a triangle always add up to $180^{\circ}$.


After drawing several different triangles, you should cut the angles out and arrange them on a straight line to see if they add up to $180^{\circ}$. You could also use a protractor (if you have one).

## SEE: lesson video here.



DO:
Find angle $a, b, c, d, e$ and $f$


Remember:
The angles in a triangle add up to $180^{\circ}$.

[^0]THINK: My friend says the angles in a quadrilateral always add up to $360^{\circ}$.


Rectangle
All angles $90^{\circ}$ Opposite sides equal


Square All angles $90^{\circ}$ All sides equal


Rhombus All sides equal Opposite side pposite sid
parallel


Parallelogram
Opposite sides parallel
and equal


Trapezoid (US) Trapezium (UK)

Two sides parallel


Kite Adjacent pairs of sides equal

After drawing several different quadrilaterals, you could cut the quadrilaterals into triangles using one cut and you could also use a protractor (if you have one).
Tip: Yesterday we learnt that the sum of the angles in a triangle is $180^{\circ}$. Does this help?
SEE: lesson video here.


I can see that quadrilaterals can be split into two triangles by drawing a straight line from one vertex to another. If the angles in a triangle add up to $1 \mathbf{8 0}^{\circ}$ then quadrilaterals (two triangles) must have interior angles adding up to $360^{\circ}$.

When I cut the angles out and join them together they make a full circle WHICH IS $360^{\circ}$.
When I use a protractor to measure the angles in a quadrilateral, I find THEY ADD UP TO $360^{\circ}$. (if you are wrong by one or two degrees, that is very normal - $358^{\circ}$ to $362^{\circ}$ is accurate enough to show that the angle add up to $360^{\circ}$ )

## MAKING CONNECTIONS:

Squares have 4 equal angles and each angle is $90^{\circ}$ because $360 \div 4=90$
Parallelograms have opposite angles which are equal so I only need to know one angle to find them all see here to explore this further.

DO: Find angle $a, b, c, d, e$ and $f$


## Remember:

The angles in a quadrilateral add up to $360^{\circ}$. Look for angles that are equal.
Look for angles that measure $90^{\circ}$.

THINK: My friend thinks she can work out the size of angles in regular pentagons and hexagons without a protractor.


Yesterday, we learnt that the sum of the angles in a quadrilateral is $360^{\circ}$.
Tuesday, we learnt that the sum of the angles in a triangle is $180^{\circ}$.
Tip: Try drawing regular pentagons and hexagons using triangles and quadrilaterals
SEE: lesson video here.


5-sides 3 triangles

## A pentagon is made up of $\mathbf{3}$ triangles <br> Angles in a triangle ADD UP TO $18 \mathbf{0}^{\circ}$.

$180 \times 3=540$ so the angles in a pentagon must add up to $540^{\circ}$
If the angles in a pentagon add up to $540^{\circ}$ and there are 5 equal angles in a regular pentagon then each angle must be $120^{\circ}$ because $540 \div 5=108$

When I use a protractor to measure the angles in a reglular pentagon, I find are all $108^{\circ}$.
A hexagon is made up of 4 triangles and angles in a triangle ADD UP TO $18 \mathbf{1 0}^{\circ}$.
$4 \times 180=\mathbf{7 2 0}$ so the angles in a hexagon must add up to $720^{\circ}$.
If the angles in a hexagon add up to $720^{\circ}$ and there are 6 equal angles in a regular hexagon then each angle must be $120^{\circ}$ because $\mathbf{7 2 0} \div \mathbf{6 = 1 2 0}$

When I use a protractor to measure the angles in a reglular hexagon, I find are all $120^{\circ}$.

## Making connections:

- I can also see that a hexagon is made up of two quadrilaterals (which is the same as 4 triangles) and a pentagon is made up of 1 quadrilateral and one triangle (which is the same as 3 triangles)
- Shapes with more than three sides can all be divided into triangles.
the number of sides minus $2=$ the number of triangles
Explore more here


## DO:

Solve these problems
two triangles have been done for you already.


1. Find the sum of the interior angles of a regular octagon.
2. Find the size of each interior angle in a regular octagon

TOP TIPS
Choose a vertex and draw a line to another vertex to create a triangle. Repeat with the same vertex until you have joined it to all the vertex you can. Count how many triangles you have made.
Q) 3, 4 and 5


## Find:

3) $d+e+f$
4) $b+c+d$
5) $a+b+c+d+e+f+g+h+i$

THINK: What is the relationship between the diameter and the radius? What kind of triangle is created inside the circle on the right (below)? Why?


Tip: An isosceles triangle is a triangle with two equal sides and two equal angles. What is the connection to the circle above (on the right)?
SEE: lesson video here. and further information here


180-38-38=104


- The Radius is the distance from the centre outwards.
- The Diameter goes straight across the circle, through the centre.
- The diameter is always double the length of the radius.
- The triangle is an isosceles triangle because two of the sides are the same length (because they are radii). Because of this, two of the angles are the same. See more here
- Knowing this can help us to solve problems involving circles.


## DO:

Solve these problems

3) Find the missing angles


## ANSWERS:

Day 1


## ANSWERS:

| Day 2 | Day 3 | Day 4 | Day 5 |
| :---: | :---: | :---: | :---: |
| $a=103^{\circ}$ | $a=87^{\circ}$ | 1) $1080^{\circ}$ - An octagon is made up of 6 | 1) 3.6 cm |
| $b=65^{\circ}$ | $b=133^{\circ}$ | trangle | 2) 35 mm |
| c $=126^{\circ}$ | $C=116^{\circ}$ | 2) $135^{\circ}$ - An octagon has eight equal angles so $1080 \div 8=135$ |  |
|  |  |  | $t=31^{\circ}$ |
| $d=27^{\circ}$ | $d=64{ }^{\circ}$ | 3) $180^{\circ}$ | $s=118^{\circ}$ |
|  |  |  | $\mathrm{u}=70^{\circ}$ |
| $\mathrm{e}=38^{\circ}$ | $e=116^{\circ}$ | 4) $180^{\circ}$ |  |
| $\mathrm{f}=71^{\circ}$ |  |  |  |
|  | $\mathrm{f}=137^{\circ}$ | 5) $540^{\circ}$ | $\begin{aligned} & x=80^{\circ} \\ & y=50^{\circ} \end{aligned}$ |
|  |  |  | $\mathrm{z}=50^{\circ}$ |


[^0]:    Explore this website for more information about triangles.

